Logistic Regression

BUS 735: Business Decision Making and Research

Specific goals:

- Learn how to conduct regression analysis with a dummy independent variable.
- Learning objectives:
 - LO2: Be able to construct and use multiple regression models (including some limited dependent variable models) to construct and test hypotheses considering complex relationships among multiple variables.
 - LO6: Be able to use standard computer packages such as SPSS and Excel to conduct the quantitative analyses described in the learning objectives above.
 - LO7: Have a sound familiarity of various statistical and quantitative methods in order to be able to approach a business decision problem and be able to select appropriate methods to answer the question.

Specific goals:

 Learn how to conduct regression analysis with a dummy independent variable.

Learning objectives:

- LO2: Be able to construct and use multiple regression models (including some limited dependent variable models) to construct and test hypotheses considering complex relationships among multiple variables.
- LO6: Be able to use standard computer packages such as SPSS and Excel to conduct the quantitative analyses described in the learning objectives above.
- LO7: Have a sound familiarity of various statistical and quantitative methods in order to be able to approach a business decision problem and be able to select appropriate methods to answer the question.

- Logistic Regression: method for estimating a regression with a dummy dependent variable.
- Will a potential customer purchase a product? (YES=1, NO=0).
 - Might use explanatory variables: age, gender, income, etc.
- Will a potential employee be retained after one year? (YES=1, NO=0).
 - Might use explanatory variables: age, gender, years experience, past income, education dummy (4-year = 1, otherwise = 0).
- Why not run a regression? Which assumption is violated?

- Logistic Regression: method for estimating a regression with a dummy dependent variable.
- Will a potential customer purchase a product? (YES=1, NO=0).
 - Might use explanatory variables: age, gender, income, etc.
- Will a potential employee be retained after one year? (YES=1, NO=0).
 - Might use explanatory variables: age, gender, years experience, past income, education dummy (4-year = 1, otherwise = 0).
- Why not run a regression? Which assumption is violated?

- Logistic Regression: method for estimating a regression with a dummy dependent variable.
- Will a potential customer purchase a product? (YES=1, NO=0).
 - Might use explanatory variables: age, gender, income, etc.
- Will a potential employee be retained after one year? (YES=1, NO=0).
 - Might use explanatory variables: age, gender, years experience, past income, education dummy (4-year = 1, otherwise = 0).
- Why not run a regression? Which assumption is violated?

- Logistic Regression: method for estimating a regression with a dummy dependent variable.
- Will a potential customer purchase a product? (YES=1, NO=0).
 - Might use explanatory variables: age, gender, income, etc.
- Will a potential employee be retained after one year? (YES=1, NO=0).
 - Might use explanatory variables: age, gender, years experience, past income, education dummy (4-year = 1, otherwise = 0).
- Why not run a regression? Which assumption is violated?

- **Logistic Regression**: method for estimating a regression with a *dummy dependent variable*.
- Will a potential customer purchase a product? (YES=1, NO=0).
 - Might use explanatory variables: age, gender, income, etc.
- Will a potential employee be retained after one year? (YES=1, NO=0).
 - Might use explanatory variables: age, gender, years experience, past income, education dummy (4-year = 1, otherwise = 0).
- Why not run a regression? Which assumption is violated?

- Logistic Regression: method for estimating a regression with a *dummy dependent variable*.
- Will a potential customer purchase a product? (YES=1, NO=0).
 - Might use explanatory variables: age, gender, income, etc.
- Will a potential employee be retained after one year? (YES=1, NO=0).
 - Might use explanatory variables: age, gender, years experience, past income, education dummy (4-year = 1, otherwise = 0).
- Why not run a regression? Which assumption is violated?
 Dependent variable is not interval. As a result, residual will not be normally distributed.

$$y_i = b_0 + b_1 X_{1,i} + b_2 X_{2,i} + \dots + b_{k-1} X_{k-1,i} + e_i$$

Logistic regression:

$$\log(Odds) = b_0 + b_1 X_{1,i} + b_2 X_{2,i} + \dots + b_{k-1} X_{k-1,i} + e_i$$

$$Odds = \frac{P(y_i = 1)}{1 - P(y_i = 1)} = \frac{P(y_i = 1)}{P(y_i = 0)}$$

 Remember, y_i ∈ 0,1 indicates YES=1 event did occur, or NO=0 event did not occur.

$$y_i = b_0 + b_1 X_{1,i} + b_2 X_{2,i} + ... + b_{k-1} X_{k-1,i} + e_i$$

Logistic regression:

$$\log(Odds) = b_0 + b_1 X_{1,i} + b_2 X_{2,i} + \dots + b_{k-1} X_{k-1,i} + e_i$$

$$Odds = \frac{P(y_i = 1)}{1 - P(y_i = 1)} = \frac{P(y_i = 1)}{P(y_i = 0)}$$

• Remember, $y_i \in 0,1$ indicates YES=1 event did occur, or NO=0 event did not occur

$$y_i = b_0 + b_1 X_{1,i} + b_2 X_{2,i} + ... + b_{k-1} X_{k-1,i} + e_i$$

Logistic regression:

$$\log(Odds) = b_0 + b_1 X_{1,i} + b_2 X_{2,i} + \dots + b_{k-1} X_{k-1,i} + e_i$$

$$Odds = \frac{P(y_i = 1)}{1 - P(y_i = 1)} = \frac{P(y_i = 1)}{P(y_i = 0)}$$

• Remember, $y_i \in 0,1$ indicates YES=1 event did occur, or NO=0 event did not occur.

$$y_i = b_0 + b_1 X_{1,i} + b_2 X_{2,i} + ... + b_{k-1} X_{k-1,i} + e_i$$

Logistic regression:

$$\log(Odds) = b_0 + b_1 X_{1,i} + b_2 X_{2,i} + \dots + b_{k-1} X_{k-1,i} + e_i$$

$$Odds = \frac{P(y_i = 1)}{1 - P(y_i = 1)} = \frac{P(y_i = 1)}{P(y_i = 0)}$$

• Remember, $y_i \in 0,1$ indicates YES=1 event did occur, or NO=0 event did not occur

$$y_i = b_0 + b_1 X_{1,i} + b_2 X_{2,i} + ... + b_{k-1} X_{k-1,i} + e_i$$

Logistic regression:

$$\log(Odds) = b_0 + b_1 X_{1,i} + b_2 X_{2,i} + \dots + b_{k-1} X_{k-1,i} + e_i$$

$$Odds = \frac{P(y_i = 1)}{1 - P(y_i = 1)} = \frac{P(y_i = 1)}{P(y_i = 0)}$$

• Remember, $y_i \in 0,1$ indicates YES=1 event did occur, or NO=0 event did not occur.

$$y_i = b_0 + b_1 X_{1,i} + b_2 X_{2,i} + ... + b_{k-1} X_{k-1,i} + e_i$$

Logistic regression:

$$\log(Odds) = b_0 + b_1 X_{1,i} + b_2 X_{2,i} + \dots + b_{k-1} X_{k-1,i} + e_i$$

$$Odds = \frac{P(y_i = 1)}{1 - P(y_i = 1)} = \frac{P(y_i = 1)}{P(y_i = 0)}$$

• Remember, $y_i \in 0,1$ indicates YES=1 event did occur, or NO=0 event did not occur.

$$\hat{y}_i = b_0 + b_1 X_{1,i} + b_2 X_{2,i} + \dots + b_{k-1} X_{k-1,i}$$

 For a logistic regression, you can get predicted logist (not too interesting yet):

$$\hat{J}_i = \widehat{In(Odds)} = b_0 + b_1 X_{1,i} + b_2 X_{2,i} + ... + b_{k-1} X_{k-1,i}$$

$$\widehat{P(y_i = 1)} = \frac{1}{1 + e^{(-\hat{l}_i)}}$$

$$\hat{y}_i = b_0 + b_1 X_{1,i} + b_2 X_{2,i} + \dots + b_{k-1} X_{k-1,i}$$

 For a logistic regression, you can get predicted logist (not too interesting yet):

$$\hat{J}_i = \widehat{In(Odds)} = b_0 + b_1 X_{1,i} + b_2 X_{2,i} + ... + b_{k-1} X_{k-1,i}$$

$$\widehat{P(y_i = 1)} = \frac{1}{1 + e^{(-\hat{I}_i)}}$$

$$\hat{y}_i = b_0 + b_1 X_{1,i} + b_2 X_{2,i} + \dots + b_{k-1} X_{k-1,i}$$

 For a logistic regression, you can get predicted logist (not too interesting yet):

$$\hat{l}_i = In(Odds) = b_0 + b_1 X_{1,i} + b_2 X_{2,i} + ... + b_{k-1} X_{k-1,i}$$

$$P(\widehat{y_i} = 1) = \frac{1}{1 + e^{(-\hat{l}_i)}}$$

$$\hat{y}_i = b_0 + b_1 X_{1,i} + b_2 X_{2,i} + \dots + b_{k-1} X_{k-1,i}$$

 For a logistic regression, you can get predicted logist (not too interesting yet):

$$\hat{l}_i = \widehat{ln(Odds)} = b_0 + b_1 X_{1,i} + b_2 X_{2,i} + ... + b_{k-1} X_{k-1,i}$$

$$P(\widehat{y_i} = 1) = \frac{1}{1 + e^{(-\hat{l}_i)}}$$

$$\hat{y}_i = b_0 + b_1 X_{1,i} + b_2 X_{2,i} + \dots + b_{k-1} X_{k-1,i}$$

 For a logistic regression, you can get predicted logist (not too interesting yet):

$$\hat{l}_i = \widehat{In(Odds)} = b_0 + b_1 X_{1,i} + b_2 X_{2,i} + ... + b_{k-1} X_{k-1,i}$$

$$\widehat{P(y_i = 1)} = \frac{1}{1 + e^{(-\hat{l}_i)}}$$

$$\hat{y}_i = b_0 + b_1 X_{1,i} + b_2 X_{2,i} + \dots + b_{k-1} X_{k-1,i}$$

 For a logistic regression, you can get predicted logist (not too interesting yet):

$$\hat{l}_i = \widehat{ln(Odds)} = b_0 + b_1 X_{1,i} + b_2 X_{2,i} + ... + b_{k-1} X_{k-1,i}$$

$$\widehat{P(y_i = 1)} = \frac{1}{1 + e^{(-\hat{l}_i)}}$$

- Marginal effect for regression: measure of how much *y* changes when *x* increases by 1.
 - Example: How much does public expenditure per capita increase (or decrease) when economic ability increases by one unit?
- Marginal effect for logit: measure of how much $P(y_i = 1)$ changes when x increases by 1.
 - How much more (or less) likely will an interview candicate be working here after one year if she/he has a four year college education?

- Marginal effect for regression: measure of how much *y* changes when *x* increases by 1.
 - Example: How much does public expenditure per capita increase (or decrease) when economic ability increases by one unit?
- Marginal effect for logit: measure of how much $P(y_i = 1)$ changes when x increases by 1.
 - How much more (or less) likely will an interview candicate be working here after one year if she/he has a four year college education?

- Marginal effect for regression: measure of how much *y* changes when *x* increases by 1.
 - Example: How much does public expenditure per capita increase (or decrease) when economic ability increases by one unit?
- Marginal effect for logit: measure of how much $P(y_i = 1)$ changes when x increases by 1.
 - How much more (or less) likely will an interview candicate be working here after one year if she/he has a four year college education?

- Marginal effect for regression: measure of how much *y* changes when *x* increases by 1.
 - Example: How much does public expenditure per capita increase (or decrease) when economic ability increases by one unit?
- Marginal effect for logit: measure of how much $P(y_i = 1)$ changes when x increases by 1.
 - How much more (or less) likely will an interview candicate be working here after one year if she/he has a four year college education?

• For a regular regression, for coefficient b_2 :

- The sign (positive/negative) indicates whether x_2 causes y to increase or decrease.
- The magnitude tells how much y increases when increasing x_2 by 1.
- Coefficient = Marginal Effect.
- For a logistic regression, the coefficient b_2 :
 - The sign (positive/negative) indicates whether x₂ causes y to increase or decrease.
 - The magnitude is pretty meaningless.
 - Need to do more to figure out marginal effect
- Because SPSS is stupid, it cannot figure out marginal effects.
- For a specific individual (specific values for X's), compute predicted probabilities by hand for:
 - The individual's actual set of values for X's
 - Same set of X's, except increase one of them by 1
 - Take the difference = Marginal effect.

- For a regular regression, for coefficient b_2 :
 - The sign (positive/negative) indicates whether x₂ causes y to increase or decrease.
 - The magnitude tells *how much y* increases when increasing x_2 by 1.
 - Coefficient = Marginal Effect.
- For a logistic regression, the coefficient b_2 :
 - The sign (positive/negative) indicates whether x₂ causes y to increase or decrease.
 - The magnitude is pretty meaningless.
 - Need to do more to figure out marginal effect
- Because SPSS is stupid, it cannot figure out marginal effects.
- For a specific individual (specific values for X's), compute predicted probabilities by hand for:
 - The individual's actual set of values for X's
 - Same set of X's, except increase one of them by 1.
 - Take the difference = Marginal effect.

- For a regular regression, for coefficient b_2 :
 - The sign (positive/negative) indicates whether x₂ causes y to increase or decrease.
 - The magnitude tells *how much y* increases when increasing x_2 by 1.
 - Coefficient = Marginal Effect.
- For a logistic regression, the coefficient b_2 :
 - The sign (positive/negative) indicates whether x₂ causes y to increase or decrease.
 - The magnitude is pretty meaningless.
 - Need to do more to figure out marginal effect
- Because SPSS is stupid, it cannot figure out marginal effects.
- For a specific individual (specific values for X's), compute predicted probabilities by hand for:
 - The individual's actual set of values for X's
 - Same set of X's, except increase one of them by 1
 - Take the difference = Marginal effect.

- For a regular regression, for coefficient b_2 :
 - The sign (positive/negative) indicates whether x₂ causes y to increase or decrease.
 - The magnitude tells *how much y* increases when increasing x_2 by 1.
 - Coefficient = Marginal Effect.
- For a logistic regression, the coefficient b_2 :
 - The sign (positive/negative) indicates whether x₂ causes y to increase or decrease.
 - The magnitude is pretty meaningless.
 - Need to do more to figure out marginal effect.
- Because SPSS is stupid, it cannot figure out marginal effects.
- For a specific individual (specific values for X's), compute predicted probabilities by hand for:
 - The individual's actual set of values for X's
 - Same set of X's, except increase one of them by 1
 - Take the difference = Marginal effect.

- For a regular regression, for coefficient b_2 :
 - The sign (positive/negative) indicates whether x₂ causes y to increase or decrease.
 - The magnitude tells *how much y* increases when increasing x_2 by 1.
 - Coefficient = Marginal Effect.
- For a logistic regression, the coefficient b_2 :
 - The sign (positive/negative) indicates whether x₂ causes y to increase or decrease.
 - The magnitude is pretty meaningless.
 - Need to do more to figure out marginal effect.
- Because SPSS is stupid, it cannot figure out marginal effects.
- For a specific individual (specific values for X's), compute predicted probabilities by hand for:
 - The individual's actual set of values for X's
 - Same set of X's, except increase one of them by 1
 - Take the difference = Marginal effect.

- For a regular regression, for coefficient b_2 :
 - The sign (positive/negative) indicates whether x₂ causes y to increase or decrease.
 - The magnitude tells *how much y* increases when increasing x_2 by 1.
 - Coefficient = Marginal Effect.
- For a logistic regression, the coefficient b_2 :
 - The sign (positive/negative) indicates whether x_2 causes y to increase or decrease.
 - The magnitude is pretty meaningless.
 - Need to do more to figure out marginal effect.
- Because SPSS is stupid, it cannot figure out marginal effects.
- For a specific individual (specific values for X's), compute predicted probabilities by hand for:
 - The individual's actual set of values for X's
 - Same set of X's, except increase one of them by 1
 - Take the difference = Marginal effect.

- For a regular regression, for coefficient b_2 :
 - The sign (positive/negative) indicates whether x₂ causes y to increase or decrease.
 - The magnitude tells *how much y* increases when increasing x_2 by 1.
 - Coefficient = Marginal Effect.
- For a logistic regression, the coefficient b_2 :
 - The sign (positive/negative) indicates whether x_2 causes y to increase or decrease.
 - The magnitude is pretty meaningless.
 - Need to do more to figure out marginal effect.
- Because SPSS is stupid, it cannot figure out marginal effects.
- For a specific individual (specific values for X's), compute predicted probabilities by hand for:
 - The individual's actual set of values for X's
 - Same set of X's, except increase one of them by 1
 - Take the difference = Marginal effect.

- For a regular regression, for coefficient b_2 :
 - The sign (positive/negative) indicates whether x₂ causes y to increase or decrease.
 - The magnitude tells *how much y* increases when increasing x_2 by 1.
 - Coefficient = Marginal Effect.
- For a logistic regression, the coefficient b_2 :
 - The sign (positive/negative) indicates whether x_2 causes y to increase or decrease.
 - The magnitude is pretty meaningless.
 - Need to do more to figure out marginal effect.
- Because SPSS is stupid, it cannot figure out marginal effects.
- For a specific individual (specific values for X's), compute predicted probabilities by hand for:
 - The individual's actual set of values for X's
 - Same set of X's, except increase one of them by 1.
 - Take the difference = Marginal effect.

- For a regular regression, for coefficient b_2 :
 - The sign (positive/negative) indicates whether x₂ causes y to increase or decrease.
 - The magnitude tells *how much y* increases when increasing x_2 by 1.
 - Coefficient = Marginal Effect.
- For a logistic regression, the coefficient b_2 :
 - The sign (positive/negative) indicates whether x_2 causes y to increase or decrease.
 - The magnitude is pretty meaningless.
 - Need to do more to figure out marginal effect.
- Because SPSS is stupid, it cannot figure out marginal effects.
- For a specific individual (specific values for X's), compute predicted probabilities by hand for:
 - The individual's actual set of values for X's.
 - Same set of X's, except increase one of them by 1
 - Take the difference = Marginal effect.

- For a regular regression, for coefficient b_2 :
 - The sign (positive/negative) indicates whether x_2 causes y to increase or decrease.
 - The magnitude tells *how much y* increases when increasing x_2 by 1.
 - Coefficient = Marginal Effect.
- For a logistic regression, the coefficient b_2 :
 - The sign (positive/negative) indicates whether x₂ causes y to increase or decrease.
 - The magnitude is pretty meaningless.
 - Need to do more to figure out marginal effect.
- Because SPSS is stupid, it cannot figure out marginal effects.
- For a specific individual (specific values for X's), compute predicted probabilities by hand for:
 - The individual's actual set of values for X's.
 - Same set of X's, except increase one of them by 1.
 - Take the difference = Marginal effect.

- For a regular regression, for coefficient b_2 :
 - The sign (positive/negative) indicates whether x₂ causes y to increase or decrease.
 - The magnitude tells *how much y* increases when increasing x_2 by 1.
 - Coefficient = Marginal Effect.
- For a logistic regression, the coefficient b_2 :
 - The sign (positive/negative) indicates whether x₂ causes y to increase or decrease.
 - The magnitude is pretty meaningless.
 - Need to do more to figure out marginal effect.
- Because SPSS is stupid, it cannot figure out marginal effects.
- For a specific individual (specific values for X's), compute predicted probabilities by hand for:
 - The individual's actual set of values for X's.
 - Same set of X's, except increase one of them by 1.
 - Take the difference = Marginal effect.

- For a regular regression, for coefficient b_2 :
 - The sign (positive/negative) indicates whether x₂ causes y to increase or decrease.
 - The magnitude tells *how much y* increases when increasing x_2 by 1.
 - Coefficient = Marginal Effect.
- For a logistic regression, the coefficient b_2 :
 - The sign (positive/negative) indicates whether x₂ causes y to increase or decrease.
 - The magnitude is pretty meaningless.
 - Need to do more to figure out marginal effect.
- Because SPSS is stupid, it cannot figure out marginal effects.
- For a specific individual (specific values for X's), compute predicted probabilities by hand for:
 - The individual's actual set of values for X's.
 - Same set of X's, except increase one of them by 1.
 - Take the difference = Marginal effect.

- For a regular regression, for coefficient b_2 :
 - The sign (positive/negative) indicates whether x₂ causes y to increase or decrease.
 - The magnitude tells *how much y* increases when increasing x_2 by 1.
 - Coefficient = Marginal Effect.
- For a logistic regression, the coefficient b_2 :
 - The sign (positive/negative) indicates whether x₂ causes y to increase or decrease.
 - The magnitude is pretty meaningless.
 - Need to do more to figure out marginal effect.
- Because SPSS is stupid, it cannot figure out marginal effects.
- For a specific individual (specific values for X's), compute predicted probabilities by hand for:
 - The individual's actual set of values for X's.
 - Same set of X's, except increase one of them by 1.
 - Take the difference = Marginal effect.

- Well Being Dataset (Described on pages 356-357 of SAB).
- 182 college students in Washington, D.C. area.
- Variables of interest:
 - Weight (4 categories: UNDERWEIGHT=1, NORMAL=2, OVERWEIGHT=3, OBESE=4)
 - Gender (2 categories: MALE=0, FEMALE=1)
 - Age
 - Race (AFRICAN AMERICAN=1, WHITE=2, OTHER=3)
 - Marital Status (SINGLE=1, MARRIED=2, OTHER=3)
 - Financial Status (OVEREXTENDED=1, MAKING ENDS MEET=2, COMFORTABLE=3)
 - Physical Health (5 point Likert scale)
 - Depression Scale (0-60, values > 15 indicate depression)
- Find preliminary evidence whether each variable is related to weight.
- Logistic Regression Analysis.

