Transportation Models Assignment Models

Transportation Models

BUS 735: Business Decision Making and Research

Thursday, December 2, 2010

• Specific Goals:

- Learn how to formulate models involving transporting goods from suppliers to destinations.
- Learn how to use the transportation model framework for finding optimal assignments.
- Continue to perfect our linear programming / Excel skills!

• Learning Objectives:

- Be able to construct and solve linear programming models to answer business optimization problems.
- Be able to use standard computer packages such as SPSS and Excel to conduct the quantitative analyses described in the learning objectives above.

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- Transportation Models: class of problems involving transporting goods from suppliers to destinations, usually at minimum cost.
- Assumptions:
 - Each source has a fixed supply (not essential).
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- We have three different grain elevators scattered around the Great Plains that can supply grain:
 - Kansas City supplies 150 tons of grain.
 - Omaha supplies 175 tons of grain.
 - Oes Moines supplies 275 tons of grain.
- We have three different grain mills that need grain:
 - Chicago needs 200 tons of grain.
 - St. Louis needs 100 tons of grain.
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Transportation Costs

Differing distances between locations, and different gasoline prices along the routes, lead to different costs for transportation.

	Destination Cities			
Source Cities	(A) Chicago	(B) St. Louis	(C) Cincinnati	
(1) Kansas City	\$6	\$8	\$10	
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• A **balanced transportation model** is one where total demand is equal to total supply.

- $\, \bullet \,$ All supplies will be used $\, \rightarrow \,$ supply constraints have =.
- $\, \bullet \,$ All demands are satisfied $\, \rightarrow \,$ demand constraints have =.
- If demand exceeds supply (unbalanced transportation model):
 - All supplies will be used \rightarrow supply constraints have =.
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- Assignment models are like transportation models, except you decide whether or to assign a source to a destination (or employee to a task).
- Decision variables are **binary**.
- Suppose you have 3 employees and 3 tasks. How many different possible assignments are there?
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 - Each assignment must get at most 1 assignee.
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- Linear programming / Sensitivity analysis: Page 103, problems 40, 41.
- Transportation models: Pages 251-252, problems 15, 16, and 17.