BUS 735: Business Decision Making and Research



#### • Specific Goals:

- Learn how to formulate models involving transporting goods from suppliers to destinations.
- Learn how to use the transportation model framework for finding optimal assignments.
- Continue to perfect our linear programming / Excel skills

#### Learning Objectives:

- Be able to construct and solve linear programming models to answer business optimization problems.
- Be able to use standard computer packages such as SPSS and Excel to conduct the quantitative analyses described in the learning objectives above.

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- Assumptions:
  - Each source has a fixed supply (not essential).
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- We have three different grain elevators scattered around the Great Plains that can supply grain:
  - Kansas City supplies 150 tons of grain.
  - ② Omaha supplies 175 tons of grain.
  - ① Des Moines supplies 275 tons of grain.
- We have three different grain mills that need grain:
  - Chicago needs 200 tons of grain
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## Transportation Costs

Differing distances between locations, and different gasoline prices along the routes, lead to different costs for transportation.

	<b>Destination Cities</b>			
Source Cities	(A) Chicago	(B) St. Louis	(C) Cincinnati	
(1) Kansas City	\$6	\$8	\$10	
(2) Omaha	\$7	\$11	\$11	
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- What are our choice variables? How many are there?
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  - All supplies will be used  $\rightarrow$  supply constraints have =
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- If demand exceeds supply (unbalanced transportation model):
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- Decision variables are binary.
- Suppose you have 3 employees and 3 tasks. How many different possible assignments are there?
- Constraints:
  - Each assignment must get at most 1 assignee.
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• Transportation models: Pages 251-252, problems 15, 16, and 17.