## Decision Making

## BUS 735: Business Decision Making and Research

Learning Objective
Learn how to simulate probability distribution
Learn how to simulate inven- Example problem in Excel. tory systems.
Learn how to simulate queuing Example problem in Excel systems.
More practice. Read Chapter 14, Homework exercises.

## Simulating Probability Distributions

- Simulation: drawing random numbers from a probability distribution.
- Monte Carlo Simulation: Use simulated data to simply compute means, standard deviations, etc.
- More complicated computations can be made based on the simulated data.


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## Example

- Suppose the MacGuys sell somewhere between 0 and 4 computers each week from their store, according to the probability distribution to the right.
- Computers sell for \$4,300 each.
- Analytically compute the mean and standard deviation for weekly demand for computers.
- Analytically compute the mean and standard deviation for weekly revenue.

Probability
Distribution:

| Demand | Prob. |
| :---: | :---: |
| 0 | 0.2 |
| 1 | 0.4 |
| 2 | 0.2 |
| 3 | 0.1 |
| 4 | 0.1 |

- Simulate data for a number of weeks, and compute these same statistics.


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## Something More Complicated

- Suppose there is an inventory cost of $\$ 50$ per computer.
- If the company falls short, the company not only fails to make a sale, but is estimated to loose $\$ 500$ in future revenue per computer, due to making a customer unhappy.
- Suppose the company orders 1 computer per week.
- Simulate demand for two years (104 weeks), simulate inventory for each week:
- Simulate revenue, adjusting for $\$ 50$ inventory cost, $\$ 500$ shortage cost.


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\begin{aligned}
& \text { Revenue }_{t}=(\$ 4,300) \min \left(\text { Inventory }_{t}, \text { Demand }_{t}\right) \\
& -(\$ 50) \text { Inventory }_{t}-(\$ 500) \max \left(\text { Demand }_{t}-\text { Inventory }_{t}, 0\right)
\end{aligned}
$$

## Queuing System Example

- A denim manufacturing facility receives yarn at varying time intervals (according to the probability distribution in the following slide).
- Then it dyes the yarn, which takes varying amounts of time according to the second probability distibution (according to the second probability distribution on the following slide)
- If a batch of yarn arrives at the facility, it is possible it must wait for the previous batch to complete.
- It is possible that facility sits not utilized while it waits for another batch of yarn to arrive.
- Calculate the mean and std dev for the total time in the facility (waiting time + dying time)
- Calculate the mean and std dev for the waiting time.
- Calculate the average number of days per month the facility is idle.


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## Queuing System Probability Distributions

Distribution of Arrival Intervals:

## Distribution of Dying Times:

| Arrival Interval | Probability |
| :---: | :---: |
| 1 day | 0.2 |
| 2 days | 0.4 |
| 3 days | 0.3 |
| 4 days | 0.1 |


| Dying Time | Probability |
| :---: | :---: |
| 0.5 days | 0.2 |
| 1 day | 0.5 |
| 2 days | 0.3 |

## Queuing System Equations

Compute the following:
(1) Simulate Interval ${ }_{i}$.
(3) Arrival $_{i}=$ Arrival $_{i-1}+$ Interval $_{i}$.
(3) Waiting $_{i}=\max \left(\right.$ Finish $_{i-1}-$ Arrival $\left._{i}, 0\right)$
(9) Idle $_{i}=\max \left(\right.$ Arrival $_{i}-$ Finish $\left._{i-1}, 0\right)$
(3) Simulate Dying ${ }_{i}$
(0) TimeSystem ${ }_{i}=$ Waiting $_{i}+$ Dying $_{i}$
(3) Finish $_{i}=$ Arrival $_{i}+$ TimeSystem $_{i}$

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- End of Chapter 14 (pages 665-666), problems 7 and 8.
- Due Tuesday, November 6, before class.
- Type up answers in a Microsoft Word file, include your Excel file.
- Upload to D2L dropbox.

